

ESSENTIALS
OF ASTROPHYSICS

PART II

LECTURE I

GALAXIES

Kant: IF MILKY WAY IS LIMITED

- DIFFUSE, FAINT ELLIPTICAL
NEBULAE → ISLAND UNIVERSES
(1750)

- CATALOGUES:

- MESSIER (1730 - 1817)
- DREYER (1852 - 1926): NEW
GENERAL CATALOG (NGC)
~ 8,000 OBJECTS

- SHAPLEY - CURTIS DEBATE (1920)

Nebulae
part of Milky Way

↓
Extragalactic
nebulae

SETTLED BY HUBBLE WITH
CEPHEID DISTANCES
IN 1923

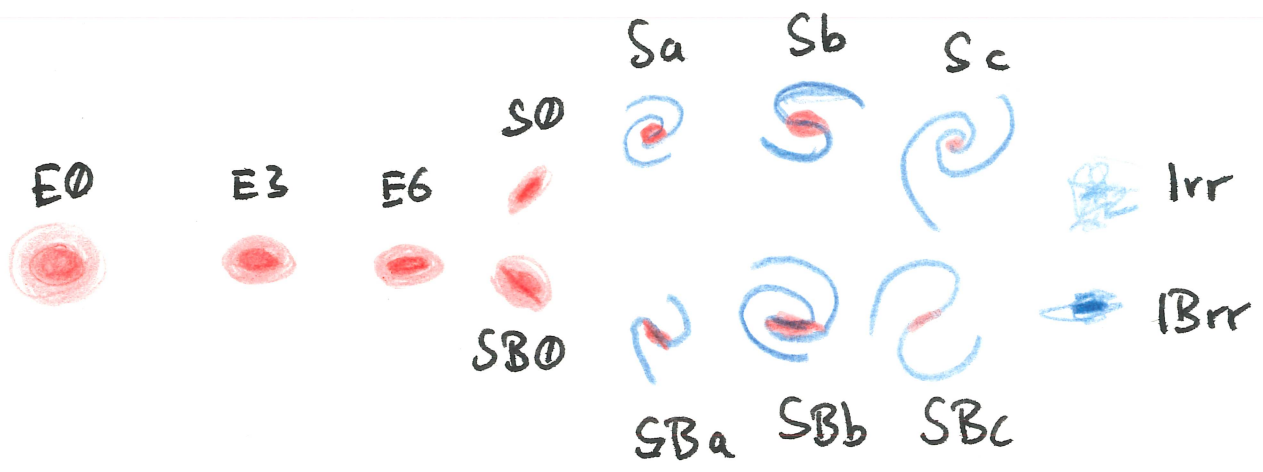
CLASSIFICATION
OF GALAXIES

- SLIDE 3 -

HUBBLE 1926 : HUBBLE SEQUENCE

- MORPHOLOGY
 - ELLIPTICALS ('E')
 - SPIRALS
 - x NORMAL SPIRALS ('S')
 - x BARRED SPIRALS ('SB')
 - Irregulars
 - TRANSITIONAL CLASS : LENTICULARS
 - x S0
 - x SB0

⇒ TUNING FORK DIAGRAM



HUBBLE

ELLIPTICALS: EARLY TYPES

SPIRALS, IRR: LATE TYPES

⚡ WRONG

⏟
NAMING STILL USED

WITHIN ELLIPTICALS:

ELLIPTICITY: $e \equiv 1 - \frac{\beta}{\alpha}$

α, β : APPARENT MAJOR AND MINOR
AXIS

HUBBLE TYPE: $10e$

SPHERICAL: E0

HIGHLY FLATTENED: E7

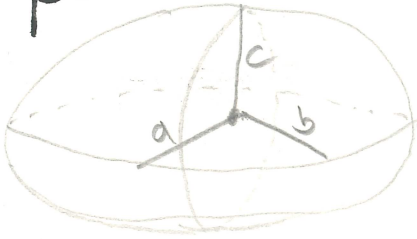
($e > 0.7$ NEVER OBSERVED)

PROBLEM: DEPENDS ON LINE OF SIGHT!

STRUCTURE OF ELLIPTICALS :

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = m^2$$

OBSERVER A OBSERVER B



OBLATE
 $a = b > c$



PROLATE
 $a = b < c$



~~ELLIPTICALS: $\frac{b}{a} = 0.6$~~

OBSERVER A: $\frac{b}{a} = 0.6 \Rightarrow E4$

OBSERVER B: $\frac{b}{a} = 1 \Rightarrow E0$

PHYSICAL PROPERTIES OF ELLIPTICALS :

B MAGNITUDES: $M_B = -8$ (DIMMEST)

$M_B = -23$ (BRIGHTEST)

blue: $\lambda = 440nm$
 $\Delta \lambda = 68nm$

$M \approx 10^7 - 10^{13} M_{\odot}$

$r \approx \mathcal{O}(10) - \mathcal{O}(100) kpc$

Masses of lenticulars SIMILAR TO ELLIPTICALS

SLIDE 4 - SLIDE 6

↑ recent bh

SLIDE 7 - 8

GENERAL STRUCTURE OF

SPIRALS

- THIN, EXTENDED GASEOUS AND STELLAR DISKS WITH STAR FORMATION IN SPIRAL ARMS

• Sa SLIDE 9

TIGHTLY WOUND SPIRAL ARMS

SMOOTH DISTRIBUTION OF STARS

MASSIVE OLD RED BRIGHT BULGE: $\frac{L_{bulge} \sim 0.3}{L_{disk}}$

• Sc SLIDE 10

LOOSE OPEN ARMS

CLUMPS OF STARS

LOW-MASS, BLUER, YOUNGER BULGE $\frac{L_{bulge} \sim 0.01}{L_{disk}}$

• Sb : TRANSITION FROM Sa - TO - Sc
SLIDE 11

ELONGATED BARS : SB

↳ DISK INSTABILITIES

SLIDE 12, 13

• SPIRALS: SMALLER PHYSICAL VARIATION

$$M_B = -16 \dots -23$$

$$M = 10^9 - 10^{12} M_0$$

$$R_{disk} \sim 5 \sim 100 \text{ kpc}$$

Irregulars:

SLIDE 14

Irr I: SOME HINT OF STRUCTURE

Irr II: DISORGANIZED

SLIDE 15

$$M_B = \dots -13 \dots -20$$

$$M \approx 10^8 \dots 10^{10} M_\odot$$

$$R \sim 1 - 10 \text{ kpc}$$

CORRELATIONS OF PHYSICAL PARAMETERS WITH GALAXY TYPES

SPIRALS AND IRREGULARS

BRIGHTNESS OF GALAXIES

~~THE~~ CORRECTIONS

ABSOLUTE MAGNITUDE OF GALAXIES:

- EXTINCTION IN MILKY WAY AND GALAXY
(SEE STARS)

• EXTINCTION NEGLECTIBLE IN EMPTY
SPACE BETWEEN GALAXIES

• REDSHIFT OF GALAXIES
(MOTION FROM EXPANSION OF UNIVERSE)

⇒

LIGHT OF B-BAND REDSHIFTED TO LONGER WAVELENGTH

↳ K-CORRECTION

• BRIGHTNESS OF BACKGROUND SKY (SUBTRACT)

$\mu_{sky} \approx 22 \frac{B-mag}{arcsec^2}$

(CCD accuracy: $29 \frac{B-mag}{arcsec^2}$)

- LIGHT POLLUTION OF CITIES
- ATMOSPHERIC EFFECTS
- ZODIACAL LIGHT (REFLECTION OF SUNS LIGHT FROM INTERPLAN. DUST)
- UNRESOLVED STARS IN MW

DE VAU COULEURS PROFILE

SURFACE BRIGHTNESS $I(r)$ [in $\frac{L_0}{pc^2}$] BULGE:

L_0 : SOLAR LUMINOSITY ($3.8 \cdot 10^{26} W$)

$$\log_{10} \left[\frac{I(r)}{I_e} \right] = -3.3307 \left[\left(\frac{r}{r_e} \right)^{1/4} - 1 \right]$$

r_e : EFFECTIVE RADIUS

I_e : $I(r_e)$

TOTAL LUMINOSITY:

$$L = \int_0^{\infty} 2\pi r I(r) dr \approx 7.22 \pi r_e^2 I_e \text{ [in } L_0 \text{]}$$

$$L(r \leq r_e) = \int_0^{r_e} 2\pi r I(r) dr = \frac{1}{2} L \text{ (DEF. OF } r_e \text{)}$$

IN $\frac{\text{mag}}{\text{arcsec}^2}$:

$$\mu(r) = \mu_e + 8.3268 \left[\left(\frac{r}{r_e} \right)^{1.4} - 1 \right]$$

GENERALIZED DE VAUCOULEUR PROFILE

SERSIC PROFILE

$$\mu(r) = \mu_e + 8.3268 \left[\left(\frac{r}{r_e} \right)^{1/n} - 1 \right]$$

μ_e, r_e, n : FREE FITTING PARAMETERS

DISK OF GALAXY: $\mu(r) = \mu_0 + 1.09 \left(\frac{r}{r_0} \right)$

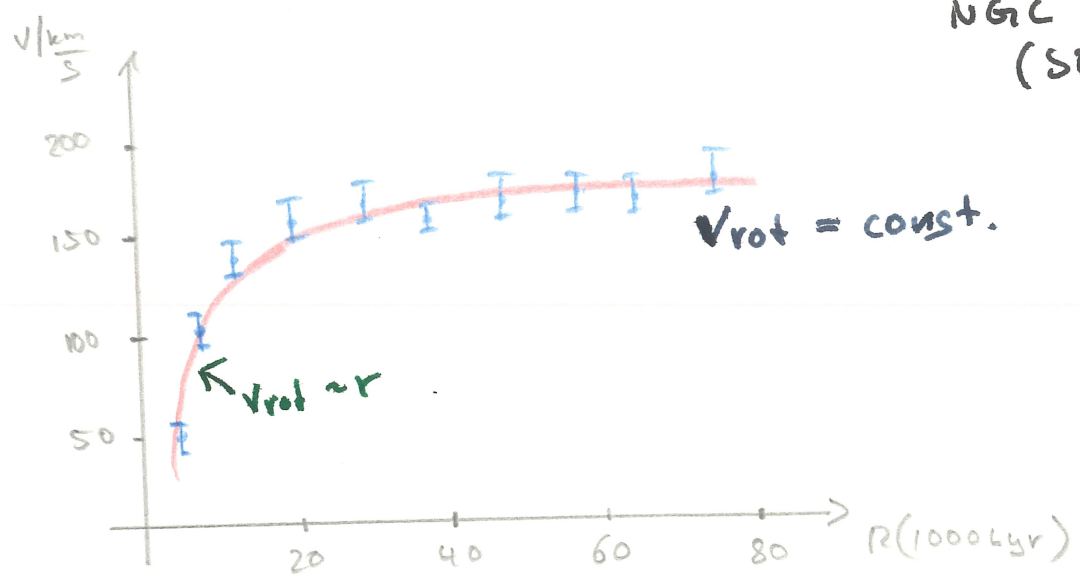
↑
char. length
scale

$n=4$: DE VAUCOULEUR

$n=1$: DISK

ROTATION CURVE OF GALAXIES

NGC 3198
(SBc)

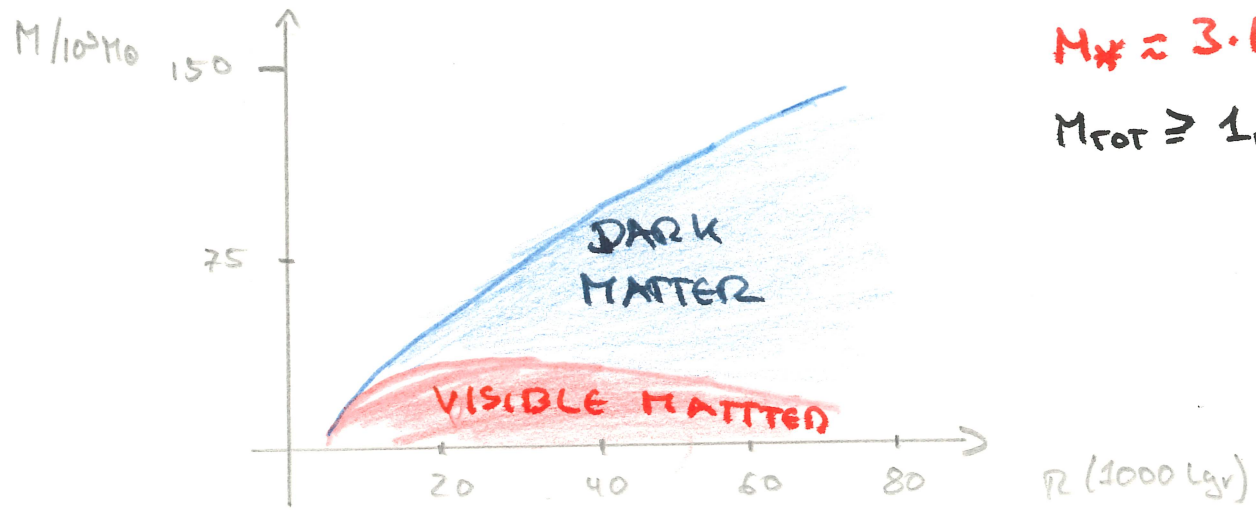


$$v_{\text{rot}}^2 = \frac{GM(r)}{r} \Rightarrow M(r) = \frac{r v_{\text{rot}}^2}{G}$$

$$v_{\text{rot}} \sim r \Rightarrow M \sim r^3$$

$$v_{\text{rot}} = \text{const.} \Rightarrow M \sim r$$

$$M(r) = 2.3 \times 10^9 \left(\frac{r}{\text{kpc}} \right) \left(\frac{v_{\text{rot}}}{100 \frac{\text{km}}{\text{s}}} \right)^2 M_{\odot}$$



$$M_{*} \approx 3 \cdot 10^{10} M_{\odot}$$

$$M_{\text{rot}} \geq 1.5 \cdot 10^{11} M_{\odot}$$

MASS DISTRIBUTION NGC 3198

TREND WITH LUMINOSITY
AND HUBBLE TYPE:

SLIDE 16

- INCREASING LUMINOSITY (L_B, M_B)
 - ⇒ ROTATION CURVE RISES MORE RAPIDLY
 - ⇒ HIGHER MAXIMUM VELOCITY
- EQUAL LUMINOSITY
 - SPIRALS OF EARLIER TYPE
 - HIGHER VELOCITY

BUT: ROTATION CURVES IN FORM
SIMILAR

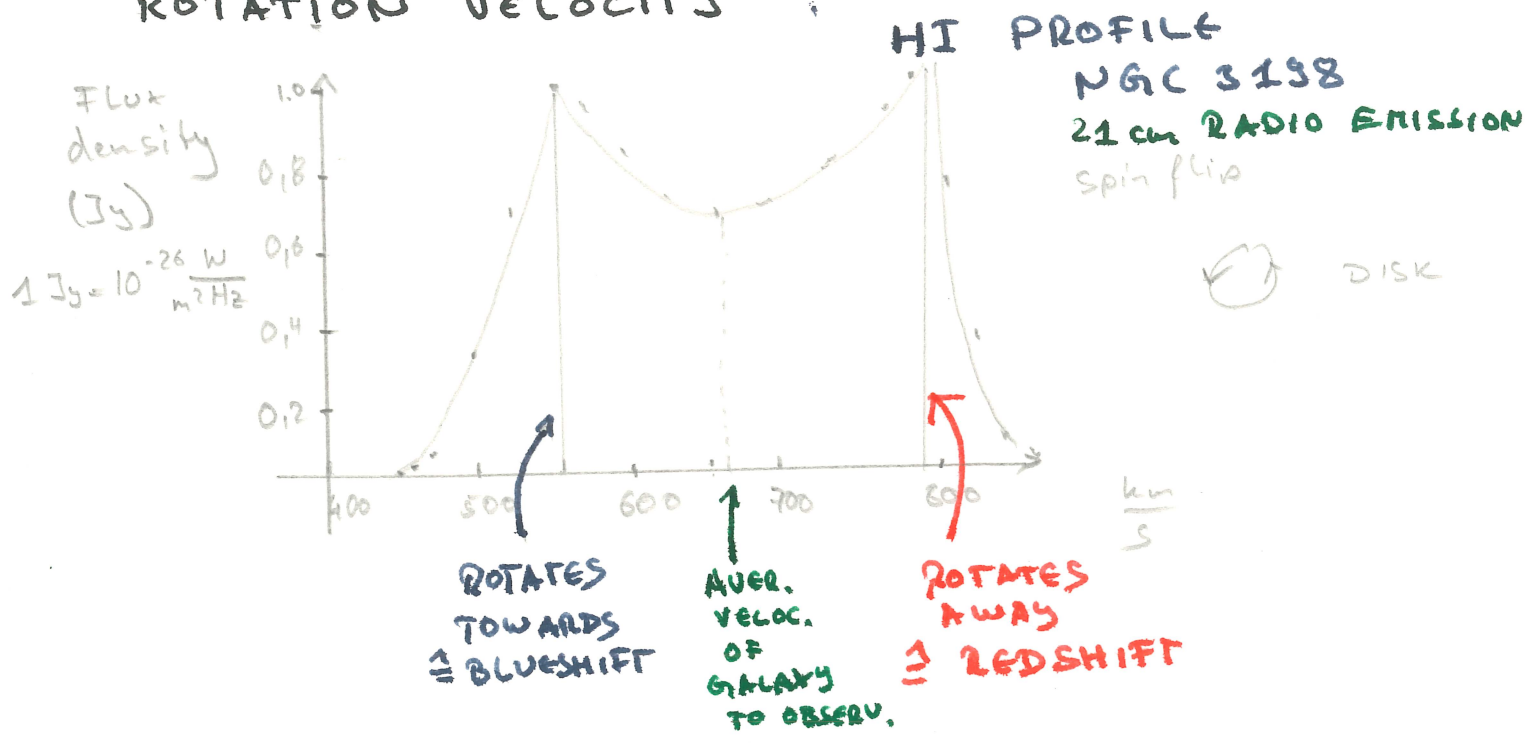
⇒ GRAVITATIONAL POTENTIAL DOES
NOT FOLLOW LUMINOUS MATTER

IRREGULAR GALAXIES: $50 < v_{max} < 70 \frac{km}{s}$

MAYBE HIGH ROTATION SPEED
REQUIRED FOR SPIRALS

TULLY - FISHER RELATION (1977)

RELATION BETWEEN LUMINOSITY OF SPIRAL GALAXY AND MAXIMUM ROTATION VELOCITY



$$\frac{\Delta \lambda}{\lambda_{\text{rest}}} \approx \frac{v_r}{c} = \frac{v \sin i}{c}$$

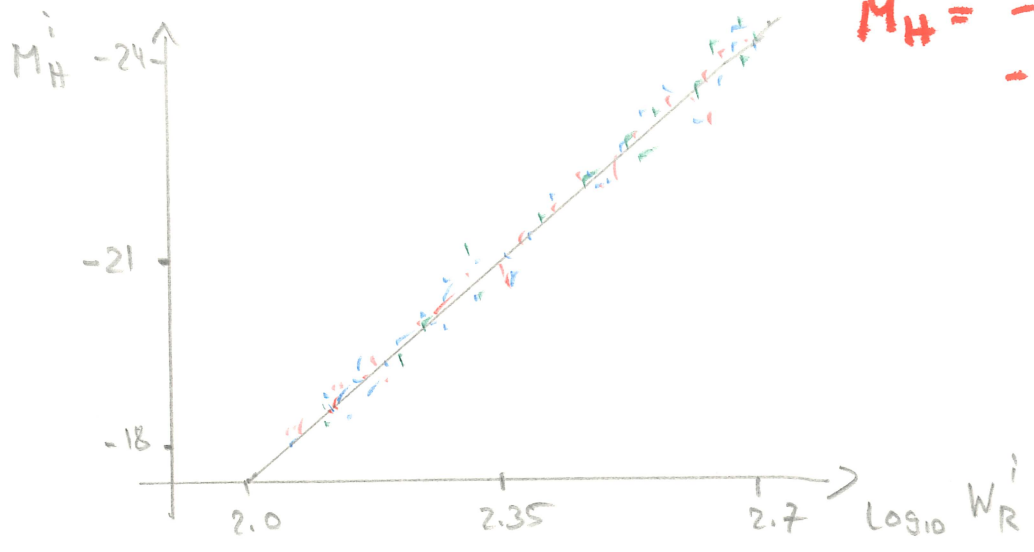
i: INCLINATION OF LINE OF SIGHT AND DIRECTION \perp TO GALACTIC PLANE

Sa: $M_B = -9.55 \log_{10} V_{\text{max}} + 3.15$

Sb: $M_B = -10.2 \log_{10} V_{\text{max}} + 2.17$

Sc: $M_B = -11.0 \log_{10} V_{\text{max}} + 3.31$

BETTER MEASURED IN INFRARED
H-BAND (1.66 μm)



$$M_H^i = -9.50 (\log_{10} W_R^i - 2.5) - 21.67 \pm 0.08$$

$$W_R^i = (W_{20} - W_{rand}) / \sin i$$

W₂₀: ΔV (Blue-ted) 20% OF PEAK

W_{rand}: Random velocity's

$$M = \frac{V_{max}^2 R}{G}$$

MASS-TO-LIGHT RATIO FOR SPIRALS:

$$\frac{M}{L} \equiv \frac{1}{C_{ML}}$$

(SAME FOR ALL SPIRALS)

$$\Rightarrow L = C_{ML} \frac{V_{max}^2 R}{G} \Rightarrow R = \frac{L G}{C_{ML} V_{max}^2}$$

ASSUME: ALL SPIRALS SAME SURFACE BRIGHTNESS AT CENTRE:

$$\frac{L}{R^2} \equiv C_{SB} \Rightarrow \frac{L C_{ML}^2 V_{max}^4}{L^2 G^2} = C_{SB}$$

$$\Rightarrow L = \frac{C_{ML}^2 V_{max}^4}{C_{SB} G^2} = C V_{max}^4$$

$L \sim V_{max}^4$

ABSOLUTE MAGNITUDE

$$\begin{aligned}
 M &= M_{\text{SUN}} - 2.5 \log_{10} \left(\frac{L}{L_{\odot}} \right) \\
 &= M_{\text{SUN}} - 2.5 \log_{10} V_{\text{max}}^4 - 2.5 \log_{10} (+2.5 \log_{10} L_{\odot}) \\
 &= -10 \log_{10} V_{\text{max}} + \text{const.}
 \end{aligned}$$

⇒ MEASURED : ≈ -9.5

⇒ SPIRAL GALAXIES HAVE
 SIMILAR M/L RATIO
 AND ROUGHLY CONSTANT
 SURFACE BRIGHTNESS

(⇒ DISTANCE TO SPIRAL GALAXY)